

**AP Calculus Definite Integral Review (Ch 4)**

Name: \_\_\_\_\_

Date: \_\_\_\_\_

1. Consider the integral  $\int_2^5 \frac{1}{x} dx$  from  $x = 2$  to  $x = 5$ . Using a Riemann sum with 6 sub-intervals calculate the area under the curve, and above the  $x$ -axis, using left endpoints. Answer to 3 decimal places.

A. 0.846                      B. 0.996                      C. 1.821                      D. 2.309

2. Consider the integral  $\int_2^6 x^2 dx$  from  $x = 2$  to  $x = 6$ . Using a Riemann sum with 4 sub-intervals calculate the area under the curve, and above the  $x$ -axis, using *midpoints*.

A. 72                              B. 66                              C. 69                              D. 58

3. Use a Trapezoidal approximation for  $\int_1^3 x^3 dx$  with  $n = 4$ .

A. 19.75                      B. 21.5                      C. 19.5                      D. 20.5

4. The following table shows selected coordinates for  $y = f(x)$ :

$x$	1	2	3	4
$y$	2.6	3.4	5.8	10.2

Given that  $f$  is continuous on  $[1, 4]$ , find a trapezoidal approximation, with  $n = 3$ , for the area under the curve from  $x = 1$  to  $x = 4$ .

5. Evaluate:  $\int \frac{2x^2 + 3x^{1/2} + 4}{x^{1/2}} dx$

A.  $\frac{4}{5}x\sqrt{x} + 2\sqrt{x} + C$       B.  $3x + \frac{4}{5}x^2\sqrt{x} + 4 + C$       C.  $3x + \frac{5}{4}x^2\sqrt{x} + 2 + C$       D.  $3x + \frac{4}{5}x^2\sqrt{2x} + 4 + C$

6. Use the Fundamental Theorem of Calculus to evaluate  $\int_2^4 x^2 dx$ .

A. -12                              B. 3                              C. 12                              D.  $\frac{56}{3}$

7. Use the Fundamental Theorem of Calculus to evaluate  $\int_{-1}^1 (\sqrt[3]{t} - 2) dt$ .

A. -4                              B.  $-\frac{5}{2}$                               C.  $-\frac{2}{3}$                               D.  $\frac{3}{2}$

8. Find the definite integral  $\int_0^3 2x(x^3 - 2x^2 + 5) dx$ .

- A.  $\frac{306}{5}$                       B.  $\frac{207}{4}$                       C.  $\frac{4}{207}$                       D. 61

9. Evaluate:  $\int_3^5 |x - 2| dx$

- A. 0                              B. 4                              C. 5                              D. 6

10. Choose the correct statement given that  $\int_0^5 f(x) dx = 7$  and  $\int_2^5 f(x) dx = -1$ .

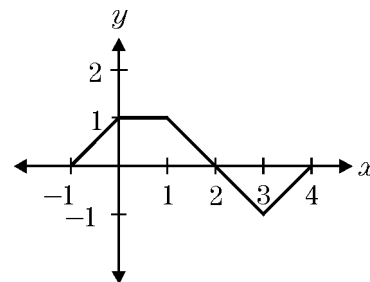
- A.  $\int_0^2 f(x) dx = 6$               B.  $\int_5^2 f(x) dx = -1$               C.  $\int_0^2 f(x) dx = 8$               D.  $\int_2^0 f(x) dx = -6$

11. Which of the following is a correct statement if  $\int_0^9 f(x) dx = 5$  and  $\int_3^9 f(x) dx = -1$ ?

- A.  $\int_3^0 f(x) dx = 6$               B.  $\int_9^3 f(x) dx = -1$               C.  $\int_0^3 f(x) dx = 4$               D.  $\int_0^3 f(x) dx = 6$

12. The graph of  $f$  is shown for  $-1 \leq x \leq 4$ . What is the value of  $\int_{-1}^4 f(x) dx$ ?

- A. 1                              B. 3                              C. 4                              D. 0



13. If  $\int_1^5 f(x) dx = 3$  and  $\int_1^5 g(x) dx = -9$ , then what is the value of  $\int_1^5 (2f + 3g)(x) dx$ ?

- A. 21                              B. -21                              C. -9                              D. 5

14. If  $\int_0^a x^3 dx = k$  for  $a > 0$  then, in terms of  $k$ ,  $\int_2^{a+2} (x - 2)^3 dx =$  \_\_\_\_\_

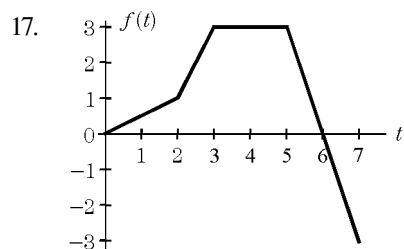
- A.  $k - 2$                               B.  $k + 2$                               C.  $k$                               D.  $8k$

15.  $\int_0^x \cos t \, dt =$

- A.  $\sin x - 1$                       B.  $\sin x + 1$                       C.  $\sin x$                       D.  $-\sin x - 1$

16. For what value(s) of  $k$  does  $\int_4^k x \, dx = 10$ ?

- A. 6 only                      B.  $\pm 6$                       C.  $2\sqrt{5}$                       D.  $\pm 2\sqrt{5}$



The graph of  $f(t)$  is shown. Fill in the table for  $F(x) = \int_0^x f(t) \, dt$ .

$x$	0	2	3	5	6	7
$F(x)$						

18. Evaluate  $\frac{d}{dx} \int_0^x (t^3 - 4t + 3) \, dt$  for  $x \geq 0$ .

- A.  $x^3 - 4$                       B.  $t^3 + 4t$                       C.  $3t^2 - 4$                       D.  $x^3 - 4x + 3$

19.  $\frac{d}{dx} \int_1^x \sqrt{3 \cos^2 t + 4} \, dt =$

- A.  $-6 \cos t \sin t$                       B.  $\sqrt{3 \cos^2 x + 4}$                       C.  $6 \cos t \sin t$                       D. 0

20.  $\frac{d}{dx} \int_x^2 \frac{5t}{2t^3 - 3} \, dt =$

- A.  $\frac{5t}{2t^3 - 3}$                       B.  $-\frac{5t}{2t^3 - 3}$                       C.  $-\frac{5x}{2x^3 - 3}$                       D.  $\frac{10}{13}$

21.  $\frac{d}{dx} \int_5^{x^3} \frac{dt}{t-7} =$

- A.  $\frac{1}{x-7}$                       B.  $-\frac{3x^2}{x^3-7}$                       C.  $\frac{3x^2}{x^3-7}$                       D.  $\frac{x^3}{x^3-7}$

22.  $\frac{d}{dx} \int_{x^3}^7 \frac{dt}{t+4} =$

- A.  $\frac{1}{x+4}$                       B.  $\frac{3x^2}{x+4}$                       C.  $-\frac{3x^2}{x^3+4}$                       D.  $\frac{x^3}{x^3+4}$

23. Let  $F(x) = \int_1^{5x+3} f(t) dt$  and  $f(13) = 4$ .

Find  $F'(2)$  by using the Fundamental Theorem of Calculus:

$$\frac{d}{dx} \int_a^b f(t) dt = f(x)$$

- A. 65                      B. 20                      C. 13                      D. -65

24. If  $F(x) = \int_0^{x^2+1} f(t) dt$  and  $f(10) = 2$ , then  $F'(3) =$

- A. 20                      B. 30                      C. 45                      D. 60

25. The average value of  $f(x) = 2x^2 - 1$  on the closed interval  $[0, 3]$  is

- A.  $\frac{17}{3}$                       B. 5                      C. 45                      D. 135

26. Find the average value of  $f(x) = \sin x$  on the interval  $[\frac{\pi}{4}, \frac{\pi}{2}]$ .

- A.  $\frac{2\sqrt{2}}{\pi}$                       B.  $\frac{\sqrt{2}}{2}$                       C.  $\frac{\sqrt{2}}{\pi}$                       D.  $\frac{2}{\pi} - \sqrt{2}$

27. A projectile moves on the  $x$ -axis so that its position is  $x(t) = -\frac{1}{2} \cos 2t + \frac{1}{2}$ , where  $t \geq 0$ . For  $0 \leq t \leq \frac{\pi}{2}$ , find the average value of the position function.

- A.  $\frac{\pi}{4}$                       B.  $\frac{1}{2}$                       C. 0                      D.  $\frac{2}{\pi}$

- |         |                     |         |   |
|---------|---------------------|---------|---|
| 1.      |                     | 21.     |   |
| Answer: | B                   | Answer: | C |
| 2.      |                     | 22.     |   |
| Answer: | C                   | Answer: | C |
| 3.      |                     | 23.     |   |
| Answer: | D                   | Answer: | B |
| 4.      |                     | 24.     |   |
| Answer: | 15.6                | Answer: | D |
| 5.      |                     | 25.     |   |
| Answer: | B                   | Answer: | B |
| 6.      |                     | 26.     |   |
| Answer: | D                   | Answer: | A |
| 7.      |                     | 27.     |   |
| Answer: | A                   | Answer: | B |
| 8.      |                     |         |   |
| Answer: | A                   |         |   |
| 9.      |                     |         |   |
| Answer: | B                   |         |   |
| 10.     |                     |         |   |
| Answer: | C                   |         |   |
| 11.     |                     |         |   |
| Answer: | D                   |         |   |
| 12.     |                     |         |   |
| Answer: | A                   |         |   |
| 13.     |                     |         |   |
| Answer: | B                   |         |   |
| 14.     |                     |         |   |
| Answer: | C                   |         |   |
| 15.     |                     |         |   |
| Answer: | C                   |         |   |
| 16.     |                     |         |   |
| Answer: | B                   |         |   |
| 17.     |                     |         |   |
| Answer: | 0, 1, 3, 9, 10.5, 9 |         |   |
| 18.     |                     |         |   |
| Answer: | D                   |         |   |
| 19.     |                     |         |   |
| Answer: | B                   |         |   |
| 20.     |                     |         |   |
| Answer: | C                   |         |   |