

Infinite Limits 27-36, 37-40

11-24.

Exer. 11-24: Find the limit, if it exists.

11. $\lim_{x \rightarrow \infty} \frac{5x^2 - 3x + 1}{2x^2 + 4x - 7}$

12. $\lim_{x \rightarrow \infty} \frac{3x^3 - x + 1}{6x^3 + 2x^2 - 7}$

13. $\lim_{x \rightarrow -\infty} \frac{4 - 7x}{2 + 3x}$

14. $\lim_{x \rightarrow -\infty} \frac{(3x + 4)(x - 1)}{(2x + 7)(x + 2)}$

15. $\lim_{x \rightarrow -\infty} \frac{2x^2 - 3}{4x^3 + 5x}$

16. $\lim_{x \rightarrow \infty} \frac{2x^2 - x + 3}{x^3 + 1}$

17. $\lim_{x \rightarrow \infty} \frac{-x^3 + 2x}{2x^2 - 3}$

18. $\lim_{x \rightarrow -\infty} \frac{x^2 + 2}{x - 1}$

19. $\lim_{x \rightarrow -\infty} \frac{2 - x^2}{x + 3}$

20. $\lim_{x \rightarrow \infty} \frac{3x^4 + x + 1}{x^2 - 5}$

21. $\lim_{x \rightarrow \infty} \sqrt[3]{\frac{8 + x^2}{x(x + 1)}}$

22. $\lim_{x \rightarrow -\infty} \frac{4x - 3}{\sqrt{x^2 + 1}}$

23. $\lim_{x \rightarrow \infty} \sin x$

24. $\lim_{x \rightarrow \infty} \cos x$

[c] Exer. 25-26: Investigate the limit by letting $x = 10^n$ for $n = 1, 2, 3$, and 4.

25. $\lim_{x \rightarrow \infty} \frac{1}{x} \tan\left(\frac{\pi}{2} - \frac{1}{x}\right)$

26. $\lim_{x \rightarrow \infty} \sqrt{x} \sin \frac{1}{x}$

Exer. 27-36: Find the vertical and horizontal asymptotes for the graph of f .

27. $f(x) = \frac{1}{x^2 - 4}$

28. $f(x) = \frac{5x}{4 - x^2}$

29. $f(x) = \frac{2x^2}{x^2 + 1}$

30. $f(x) = \frac{3x}{x^2 + 1}$

31. $f(x) = \frac{1}{x^3 + x^2 - 6x}$

32. $f(x) = \frac{x^2 - x}{16 - x^2}$

33. $f(x) = \frac{x^2 + 3x + 2}{x^2 + 2x - 3}$

34. $f(x) = \frac{x^2 - 5x}{x^2 - 25}$

35. $f(x) = \frac{x + 4}{x^2 - 16}$

36. $f(x) = \frac{\sqrt[3]{16 - x^2}}{4 - x}$

Exer. 37-40: A function f satisfies the given conditions. Sketch a possible graph for f , assuming that it does not cross a horizontal asymptote.

37. $\lim_{x \rightarrow -\infty} f(x) = 1; \quad \lim_{x \rightarrow \infty} f(x) = 1;$

$$\lim_{x \rightarrow 3^-} f(x) = -\infty; \quad \lim_{x \rightarrow 3^+} f(x) = \infty$$

38. $\lim_{x \rightarrow -\infty} f(x) = -1; \quad \lim_{x \rightarrow \infty} f(x) = -1;$

$$\lim_{x \rightarrow 2^-} f(x) = \infty; \quad \lim_{x \rightarrow 2^+} f(x) = -\infty$$

39. $\lim_{x \rightarrow -\infty} f(x) = -2; \quad \lim_{x \rightarrow \infty} f(x) = -2;$

$$\lim_{x \rightarrow 3^-} f(x) = \infty; \quad \lim_{x \rightarrow 3^+} f(x) = -\infty;$$

$$\lim_{x \rightarrow -1^-} f(x) = -\infty; \quad \lim_{x \rightarrow -1^+} f(x) = \infty$$

40. $\lim_{x \rightarrow -\infty} f(x) = 3; \quad \lim_{x \rightarrow \infty} f(x) = 3;$

$$\lim_{x \rightarrow 1^-} f(x) = \infty; \quad \lim_{x \rightarrow 1^+} f(x) = -\infty;$$

$$\lim_{x \rightarrow -2^-} f(x) = -\infty; \quad \lim_{x \rightarrow -2^+} f(x) = \infty$$

41. Salt water of concentration 0.1 pound of salt per gallon flows into a large tank that initially contains 50 gallons of pure water.

(a) If the flow rate of salt water into the tank is 5 gallons per minute, find the volume $V(t)$ of water and the amount $A(t)$ of salt in the tank after t minutes.

(b) Find a formula for the salt concentration $c(t)$ (in lb/gal) after t minutes.

(c) What happens to $c(t)$ over a long period of time?

42. An important problem in fishery science is predicting next year's adult breeding population R (the recruits) from the number S that are presently spawning. For some species (such as North Sea herring), the relationship between R and S is given by $R = aS/(S + b)$, where a and b are positive constants. What happens as the number of spawners increases?

35. $x = 4, y = 0$ 36. $x = 4, y = 0$ (37-40 Discuss in class)

31. $x = 0, x = 2, x = -3, y = 0$ 32. $x = 4, x = -4, y = -1$ 33. $x = -3, x = 1, y = 1$ 34. $x = -5, y = 1$

23. DNE 24. DNE 27. $x = 2, x = -2, y = 0$ 28. $x = 2, x = -2, y = 0$ 29. $y = 2$ 30. $y = 0$

11. $5/2, 12, 4/3, 13, -7/3, 14, 3/2, 15, 0, 16, 0, 17, -\infty, 18, -\infty, 19, \infty, 20, \infty, 21, 1, 22, -4$