

Variables and Expressions

Name _____



1. Assuming values of n for which these expressions are defined, the expression

$$\left(1 + \frac{1}{n}\right) \div \left(\frac{n+1}{n^2}\right) \text{ is equivalent to}$$

- [1] $\frac{(n+1)^2}{n^3}$ [2] $\frac{2n}{n+1}$ [3] $\frac{n^2}{n+1}$ [4] n

2. The sum $\frac{3}{x-3} + \frac{x}{3-x}$ is equivalent to

- [1] 1 [2] 0 [3] -1 [4] $\frac{x+3}{x-3}$

3. The expression $\frac{6}{z-5} - \frac{z+5}{z^2-25}$ is equivalent to

- [1] $\frac{5}{z+5}$ [2] $\frac{5z}{z-5}$ [3] $\frac{5z}{z+5}$ [4] $\frac{5}{z-5}$

4. The expression $\frac{\frac{3x}{x+3}}{\frac{x}{x^2-9}}$ is equivalent to

- [1] $3x - 9$ [2] $2x + 6$ [3] $3x$ [4] $\frac{3}{x+3}$

5. The fraction $\frac{b + \frac{b}{a}}{a - \frac{1}{a}}$ is equivalent to

- [1] b [2] $\frac{b}{a-1}$ [3] $\frac{2ab}{a^2-1}$ [4] $\frac{a-1}{b}$

6. Factor completely: $a^2 + ab + ac + bc$

- [1] $(a+b)(a+c)$ [2] $a(a+b+2c)$ [3] $a(a+b+c) + b$ [4] $(a-c)(a-b)$

7. Factor completely: $2x^2 - 18x - 72$

- [1] $2(x^2 - 9x - 36)$ [2] $2(x+3)(x-12)$ [3] $2(x-3)(x+12)$ [4] $-2(x+3)(x-12)$

1. _____
2. _____
3. _____
4. _____
5. _____
6. _____
7. _____

8. Factor completely: $3m^4 - 75$

[1] $3(m^2 + 5)(m^2 - 5)$

[2] $3m^2(m + 5)(m - 5)$

[3] $3(m^2 + 5)(m - 2)(m + 3)$

[4] $3(m^2 - 5)^2$

8. _____

9. Factor completely: $x^8 - y^4$

[1] $(x^4 + y^2)(x^4 - y^2)$

[2] $(x^4 + y^2)(x^2 - y)(x^2 + y)$

[3] $(x^4 + y^2)(x^2 + y)(x^2 - y)$

[4] $(x^2 + y)(x^2 + y)(x^2 + y)(x^2 - y)$

9. _____

10. Factor completely: $5x^2 - 20$

[1] $(5x - 4)(x + 5)$

[2] $5(x - 1)(x + 4)$

[3] $(5x + 2)(x - 10)$

[4] $5(x - 2)(x + 2)$

10. _____

11. The sum of $(y - 5) + \frac{3}{y + 2}$ is

[1] $\frac{y^2 - 7}{y + 2}$

[2] $\frac{y - 2}{y + 2}$

[3] $\frac{y^2 - 3y - 7}{y + 2}$

[4] $y - 5$

11. _____

12. The expression $\frac{2x}{x^2 - 4} \div \frac{4}{x^2 - 4x + 4} + \frac{12}{x^2 - 4} \cdot \frac{2 - x}{3}$ is equivalent to

[1] $\frac{x - 4}{2}$

[2] $\frac{x - 2}{4}$

[3] $\frac{x^2 - 2x + 8}{2x + 4}$

[4] $\frac{x^2 - 2x + 8}{2x - 4}$

12. _____

13. Expressed as a single fraction, $\frac{1}{x + 1} + \frac{1}{x}$, $x \neq 0, -1$ is

[1] $\frac{3}{x^2}$

[2] $\frac{2x + 3}{x^2 + x}$

[3] $\frac{2x + 1}{x^2 + x}$

[4] $\frac{2}{2x + 1}$

13. _____

14. In a science experiment, when resistors A and B are connected in a parallel circuit, the

total resistance is $\frac{1}{\frac{1}{A} + \frac{1}{B}}$. This complex fraction is equivalent to

[1] 1

[2] $A + B$

[3] AB

[4] $\frac{AB}{A + B}$

14. _____

15. The equation $\frac{x - 2}{x + 7} \div \frac{x + 7}{x - 2} = 1$ is true for all rational values of x where x is not equal to

[1] 2

[2] -7

[3] 2 and -7

[4] -2 and 7

15. _____

16. Factor completely: $6x^2 + 19x + 10$

[1] $(6x + 2)(x + 5)$

[3] $(3x + 2)(2x + 5)$

[2] $(6x + 5)(x + 2)$

[4] $(3x + 5)(2x + 2)$

16. _____

17. The fraction $\frac{xy^{-1} + 1}{2 + x^{-1}}$ is equivalent to $\frac{1 + xy}{y(2x + 1)}$. (TRUE or FALSE)

[1] TRUE

[2] FALSE

17. _____

18. The expression $\frac{8y^3 - 16y^2}{2y^3 - 2y^2 - 4y}$ is equivalent to

[1] $\frac{2}{y(y+1)}$

[2] $\frac{2y}{(y+1)}$

[3] $\frac{4y}{(y+1)}$

[4] $\frac{4}{(y+1)}$

18. _____

19. Find the domain of the following expression: $\frac{x-2}{x^2+9}$

[1] $x \neq \pm 3$

[2] $x \neq \pm 3$ and $x \neq 2$

[3] $x \neq -3$

[4] all x

19. _____

20. The expression $\frac{a^4 - 81}{4a^2 + 9a - 9}$ is equivalent to

[1] $\frac{a-3}{(4a+3)}$

[2] $\frac{(a^2+9)(a-3)}{(4a+3)}$

[3] $\frac{(a^2+9)}{(4a-3)}$

[4] $\frac{(a^2+9)(a+3)}{(4a+3)}$

20. _____